# SOURCES OF NON-EQUILIBRIUM IN PLASMA MATERIALS PROCESSING\*

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- Sources of non-equilibrium in plasma processing
- Examples of non-equilibrium
  - Electron transport and electromagnetics
  - Wall chemistry and plasma kinetics
  - Electrostatics in microdischarges
- Concluding Remarks

#### SO WHAT DO WE MEAN BY (NON-)EQUILIBRIUM?

- "Non-equilibrium" in plasma processing describes many phenomena, from electron transport to chemical kinetics.
- Mathematically.....If *F* is a source function for quantity *N(t)* having damping constant *τ*, then...



## NONEQUILIBRIUM IN ELECTRON TRANSPORT

• Electron transport is governed by Boltzmann's equation, which describes non-equilibrium evolution of EED in space and time.

$$\frac{df(\varepsilon, r, t)}{dt} = -\frac{q\vec{E}(r, t)}{m_e} \cdot \nabla_v f(\varepsilon, r, t) - \vec{v} \cdot \nabla f(\varepsilon, r, t) + \left(\frac{\partial f}{\partial t}\right)_c$$

• Should collisions and advection dominate, spatially dependent steady state time solutions are obtained.

$$\left\| \left( \frac{\partial f}{\partial t} \right)_c \right\| \approx \left| \frac{q\vec{E}}{m_e} \cdot \nabla_v f \right| \approx \left| \vec{v} \cdot \nabla f \right| >> \left| \frac{df}{dt} \right|, \quad f = F(E(t), N(t))$$

• Solutions may be adiabatic to slow changes in electric field or densities of collision partners.

#### NONEQUILIBRIUM IN ELECTRON TRANSPORT

 When collisions dissipate energy (and momentum) in distances (or times) small compared to advection, the Local Field approximation is obtained.

$$\left\| \left( \frac{\partial f}{\partial t} \right)_c \right\| \approx \left| \frac{q\vec{E}}{m_e} \cdot \nabla_v f \right| >> \left| \vec{v} \cdot \nabla f \right|, \quad f(r) = F(E(r), N(r))$$

• Non-equilibrium is only manifested by changes in E and N.

#### NONEQUILIBRIUM IN NEUTRAL (ION) TRANSPORT

• Nonequilibrium in neutral flow often results from "slip" of directed momenta at low pressure .

$$\frac{\partial N_i}{\partial t} = -\nabla \cdot \phi_i + S_i, \quad \phi_i = \rho_i v_i / m_i$$

$$\frac{\partial (\rho_i v_i)}{\partial t} = -\nabla P_i - \nabla \cdot (\rho_i v_i v_i) - \nabla \cdot \tau - \sum_j f_{ij} \alpha_{ij} (v_i - v_j) + S_i$$

$$v_j$$

• If  $\alpha_{ii} >> |v/\Delta x|$ , the velocities equilibrate and a single fluid results.

$$\frac{\partial N}{\partial t} = -\nabla \cdot \phi, \quad \phi = \rho v / m, \quad \rho = \sum_{i} \rho_{i}$$
$$\frac{\partial (\rho v)}{\partial t} = -\nabla P - \nabla \cdot (\rho v v) - \nabla \cdot \tau + S_{i}$$
$$\frac{\partial N_{i}}{\partial t} = -\nabla \cdot \phi_{i}, \quad \phi_{i} = N_{i} v - D_{i} N_{o} \nabla \left(\frac{N_{i}}{N_{o}}\right)$$

## NONEQUILIBRIUM IN CHEMICAL KINETICS

• Nonequilibrium in chemical kinetics (i.e., the source function) results from reaction rates being slow compared to convection.

$$\frac{\partial N_i}{\partial t} = -\nabla \cdot \phi_i + S_i$$
$$S_i = -N_i \sum_j N_j k_{ij} + \sum_{j,l} N_j N_l k_{jl} + (\nabla \cdot \phi_i) \gamma_i - \sum_l (\nabla \cdot \phi_l) \beta_{il}$$

• If  $S_i >> N_i(v/\Delta x)$ , densities become functions of only local thermodynamic parameters (EOS).

$$\frac{\partial N_o}{\partial t} = -\nabla \cdot N_o v, \quad N_i = f(N_o, T)$$

• Slowly varying boundary conditions such as wall passivation produce long term "nonequilibrium."

### NONEQUILIBRIUM IN ELECTROMAGNETICS

• Electromagnetics are governed by Maxwell's equations. In the frequency domain,

$$-\frac{1}{\mu} \left( \nabla \left( \nabla \cdot \overline{E} \right) + \nabla^2 \overline{E} \right) = \frac{\partial^2 \left( \varepsilon \overline{E} \right)}{\partial t^2} + \overline{J}_{plasma} + \overline{J}_{antenna}$$

• Although a quasi-steady harmonic state solution, non-equilibrium occurs through the consequences of E on plasma transport.

$$\nabla \cdot \overline{E} = \rho / \varepsilon_o = 0$$
 "Equilibrium"  
$$= \sum_i q_i \int (dN_i / dt) dt \neq 0$$
 "Nonequilibrium"

• These terms most often produce electrostatic waves.

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### NONEQUILIBRIUM IN ELECTROMAGNETICS

- Nonequilibrium often occurs through the feedback between the E-fields, electron transport and plasma generated current.
- Currents which are linearly proportional to fields...equilibrium

$$\overline{J}_{plasma}(r,t) = \sigma(r,t)\overline{E}(r,t) = \sigma_o(r,t)\overline{E}(r)\exp(i\omega t + \phi(r))$$

• Currents which have complex relationships to electron (or ion transport) initiated at remote sites...nonequilibrium

$$\overline{J}_{plasma}(r,t) = \iint G(r,t,r',t') \sigma(r',t') \overline{E}(r',t') dr' dt' = \sum_{i} q_i(N_i v_i)$$

• In ICP systems, this results in non-monotonic decay of Efields.

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• The self shielding of plasmas through the generation of self restoring electric fields provides "electrostatic" equilibrium.

$$\phi_i = -q_i \mu_i \nabla \Phi - D \nabla N_i \quad \leftrightarrow \quad -\nabla \cdot \varepsilon \nabla \Phi = \sum_i q_i N_i$$

• Self restoring electric fields ultimately produce quasineutrality and ambipolar transport.

$$\sum_{i} q_{i} N_{i} \approx 0 \quad \rightarrow \quad \phi_{i} = D_{ambipolar} \nabla N_{i}$$

 In systems where dimensions are commensurate with Debye lengths and shielding is incomplete, electrostatic nonequilibrium occurs.

## **EXAMPLES OF NON-EQUILIBRIUM**

- Electromagnetic non-equilibrium: Anomalous skin depth
- Chemical non-equilibrium: Evolving wall passivation
- Electrostatic nonequilibrium: Microdischarges



#### rf BIASED INDUCTIVELY COUPLED PLASMAS

- Inductively Coupled Plasmas (ICPs) with rf biasing are used here.
- < 10s mTorr, 10s MHz, 100s W kW, electron densities of 10<sup>11</sup>-10<sup>12</sup> cm<sup>-3</sup>.



• The wave equation is solved in the frequency domain with tensor conductivities.

$$-\nabla \left(\frac{1}{\mu}\nabla \cdot \overline{E}\right) + \nabla \cdot \left(\frac{1}{\mu}\nabla \overline{E}\right) = \frac{\partial^2 \left(\varepsilon \overline{E}\right)}{\partial t^2} + \frac{\partial \left(\overline{\overline{\sigma}} \cdot \overline{E} + \overline{J}\right)}{\partial t}$$

• The electrostatic term is addressed using a perturbation to the electron density.

$$\nabla \cdot \overline{E} = \frac{\rho}{\varepsilon} = \frac{q\Delta n_e}{\varepsilon}, \quad \Delta n_e = -\nabla \cdot \left(\frac{\overline{\overline{\sigma}} \cdot \overline{E}}{q}\right) / \left(\frac{1}{\tau} + i\omega\right)$$

 Conduction currents are kinetically derived to account for noncollisional effects.

$$\mathbf{J}_{e}(\vec{r},t) = J_{o}(\vec{r})\exp(i(\omega t + \phi_{v}(\vec{r}))) = -qn_{e}(\vec{r})\vec{v}_{e}(\vec{r})\exp(i(\omega t + \phi_{v}(\vec{r})))$$

#### • Continuum:

$$\partial \left(\frac{3}{2}n_e kT_e\right) / \partial t = S(T_e) - L(T_e) - \nabla \cdot \left(\frac{5}{2}\Phi kT_e - \overline{\overline{\kappa}}(T_e) \cdot \nabla T_e\right) + S_{EB}$$

- <u>Kinetic</u>: A Monte Carlo Simulation is used to derive  $f(\varepsilon, \vec{r}, t)$  including electron-electron collisions using electromagnetic and electrostatic fields.

#### PLASMA CHEMISTRY, TRANSPORT AND ELECTROSTATICS

• Continuity, momentum and energy equations for each species, and site balance models for surface chemistry.

$$\frac{\partial N_{i}}{\partial t} = -\nabla \cdot (N_{i} \vec{v}_{i}) + S_{i}$$

$$\frac{\partial (N_{i} \vec{v}_{i})}{\partial t} = \frac{1}{m_{i}} \nabla (kN_{i}T_{i}) - \nabla \cdot (N_{i} \vec{v}_{i} \vec{v}_{i}) + \frac{q_{i}N_{i}}{m_{i}} (\vec{E} + \vec{v}_{i} \times \vec{B}) - \nabla \cdot \overline{\mu}_{i} - \sum_{j} \frac{m_{j}}{m_{i} + m_{j}} N_{i}N_{j} (\vec{v}_{i} - \vec{v}_{j}) v_{ij}$$

$$\frac{\partial (N_{i}\varepsilon_{i})}{\partial t} + \nabla \cdot Q_{i} + P_{i}\nabla \cdot U_{i} + \nabla \cdot (N_{i}U_{i}\varepsilon_{i}) = \frac{N_{i}q_{i}^{2}v_{i}}{m_{i}(v_{i}^{2} + \omega^{2})} E^{2}$$

$$+ \frac{N_{i}q_{i}^{2}}{m_{i}v_{i}} E_{s}^{2} + \sum_{j} 3 \frac{m_{ij}}{m_{i} + m_{j}} N_{i}N_{j}R_{ij}k_{B}(T_{j} - T_{i}) \pm \sum_{j} 3N_{i}N_{j}R_{ij}k_{B}T_{j}$$

• Implicit solution of Poisson's equation.

$$\nabla \cdot \varepsilon \nabla \Phi (t + \Delta t) = - \left( \rho_s + \sum_i q_i N_i - \Delta t \cdot \sum_i (q_i \nabla \cdot \vec{\phi}_i) \right)$$

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#### FORCES ON ELECTRONS IN ICPs



• Inductive E-field provides azimuthal acceleration; depth 1-3 cm.

$$\delta = \left( m_e / \left( e^2 \mu_o n_e \right) \right)^{\frac{1}{2}}$$

Electrostatic (capacitive) penetrates (100s μm to mm)

$$\lambda_{S} \approx 10 \lambda_{D}, \lambda_{D} = \left( kT_{e} / \left( 8\pi n_{e}e^{2} \right) \right)^{1/2}$$

• Non-linear Lorentz Force  $\vec{F} = v_{\theta} \times \vec{B}_{rf}$ 



• Ref: V. Godyak, "Electron Kinetics of Glow Discharges"

• Collisional heating:

$$\lambda_{mfp} < \delta_{skin}, \quad \vec{J}_{e}(\vec{r},t) = \sigma(\vec{r},t)\vec{E}(\vec{r},t)$$

• Anomalous skin effect:

$$\begin{aligned} \lambda_{mfp} &> \delta_{skin} \\ \vec{J}_{e}(\vec{r},t) = \iint \sigma(\vec{r},\vec{r}',t,t') \vec{E}(\vec{r}',t') d\vec{r}' dt' \\ \vec{F} &= \vec{v} \times \vec{B} \end{aligned}$$

- Electrons receive (positive) and deliver (negative) power from/to the E-field.
- E-field is non-monotonic.

#### ELECTRON DENSITY: Ar, 10 mTorr, 200 W, 7 MHz



- Model is about 20% below experiments. This likely has to do with details of the sheath model.
- V. Godyak et al, J. Appl. Phys. 85, 703 (1999); private communication

#### TIME DEPENDENCE OF THE EED

- Time variation of the EED is mostly at higher energies where electrons are more collisional.
- Dynamics are dominantly in the electromagnetic skin depth where both collisional and non-linear Lorentz Forces) peak.
- The second harmonic dominates these dynamics.



#### • Ar, 10 mTorr, 100 W, 7 MHz, r = 4 cm

ANIMATION SLIDE

#### TIME DEPENDENCE OF THE EED: 2<sup>nd</sup> HARMONIC

- Electrons in skin depth quickly increase in energy and are "launched" into the bulk plasma.
- Undergoing collisions while traversing the reactor, they degrade in energy.
- Those surviving "climb" the opposite sheath, exchanging kinetic for potential energy.
- Several "pulses" are in transit simultaneously.
- Electron transport nonequilibrium!
  - Ar, 10 mTorr, 100 W, 7 MHz, r = 4 cm

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**ANIMATION SLIDE** 



• Amplitude of 2<sup>nd</sup> Harmonic

#### 2<sup>nd</sup> HARMONIC OF EED WITHOUT LORENTZ FORCE

- Excluding v x B terms, the non-linear Lorentz Force is removed.
- Electrons are alternately heated and cooled in the skin depth, out of phase with  $E_{\theta}$ , with some collisional heating.
- High energy electrons do not propagate (other than by diffusion) outside the skin layer.



• Amplitude of 2<sup>nd</sup> Harmonic

• Ar, 10 mTorr, 100 W, 7 MHz, r = 4 cm

ANIMATION SLIDE

- By decreasing frequency, B<sub>rf</sub> increases, the skin depth lengthens and NLF increases.
- Lower pressure extends the electron mean free path.
- Significant modulation extends to lower energies.



• Amplitude of 2<sup>nd</sup> Harmonic

**ANIMATION SLIDE** 

• Ar, 1 mTorr, 100 W, 3 MHz, r = 4 cm

#### TIME DEPENDENCE OF EED: 1 mTorr, 3 MHz

- At reduced pressure and frequency, the conditions for the nonlinear skin effect are fulfilled.
- The EED is essentially depleted of low energy electrons in the skin layer.



#### **ANIMATION SLIDE**

• Ar, 1 mTorr, 100 W, 3 MHz, r = 4 cm

## **COLLISIONLESS TRANSPORT ELECTRIC FIELDS**

- E<sub>θ</sub> exhibits extrema and nodes resulting from this noncollisional transport.
- "Sheets" of electrons with different phases provide current sources interfering or reinforcing the electric field for the next sheet.
- Axial transport results from  $\vec{v} \times \vec{B}_{rf}$  forces.
- Electromagnetic nonequilibrium!





**ANIMATION SLIDE** 





#### POWER DEPOSITION: POSITIVE AND NEGATIVE

• The end result is regions of positive and negative power deposition.



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## **POWER DEPOSITION vs FREQUENCY**

• The shorter skin depth at high frequency produces more layers of negative power deposition of larger magnitude.



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### TIME DEPENDENCE OF Ar IONIZATION: PRESSURE

 Although B<sub>rf</sub> may be nearly the same, at large P, v<sub>θ</sub> and meanfree-paths are smaller, leading to lower harmonic amplitudes.



## **EXAMPLES OF NON-EQUILIBRIUM**

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#### SURFACE CHEMISTRY OF Si ETCHING IN Cl<sub>2</sub> PLASMAS

 Etching of Si in Cl<sub>2</sub> plasmas proceeds by passivation of Si sites, followed by ion activated removal of SiCl<sub>n</sub> etch product.



 Etch products deposit on reactor walls. Cl atom recombination and SiCl<sub>n</sub> sticking slows on the passivated surfaces.





#### LONG TERM PASSIVATION OF WALLS

- Experimental measurements of optical emission, ion flux and etch rates during CI etching of Si have long term behavior.
- Transients are correlated with increasing film thickness on walls, reducing sticking coefficients for CI and SiCI.
- ICP, Cl<sub>2</sub>, 10 mTorr, 800 W.
- Plasma-surface chemical nonequilibrium!
- S. J. Ullal, T. W. Kim, V. Vahedi and E. S. Aydil, JVSTA 21, 589 (2003)

#### CHEMICAL NONEQUILIBRIUM: Ar/Cl<sub>2</sub> WITH WALL PASSIVATION

- Computationally contrast Ar/Cl<sub>2</sub> ICPs etching Si with SiCl<sub>2</sub> product, with/without wall passivation.
- Implement a multistep passivation model beginning with SiCl<sub>2</sub> polymerization. Higher degree of polymerization reduces CI reassociation.
- Without wall passivation:  $CI \rightarrow wall \rightarrow CI_2$ , p = 0.3
- With final wall passivation:  $CI \rightarrow wall \rightarrow CI_2$ , p = 0.01
- Ar/Cl<sub>2</sub> = 80/20, 10 mTorr, 400 W, 200 sccm

## [SiCl<sub>2</sub>] WITH/WITHOUT WALL PASSIVATION

• Without passivation, SiCl<sub>2</sub> has a longer residence time and builds to higher densities. Note momentum transfer from jetting nozzle.



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#### [SiCl<sub>2</sub>] TRANSIENT WITH/WITHOUT WALL PASSIVATION

• SiCl<sub>2</sub> initially sticks to walls in both cases. As passivation progresses, the sticking coefficient decreases.



• Passivation reduces CI losses on the walls, increasing its density and making pumping the largest loss.



## [CI] TRANSIENT WITH WALL PASSIVATION

• When walls are clean, CI reassociation is a large sink. As the walls passivate, surface losses decrease (except to wafer).



 Without passivation, Cl<sub>2</sub> has sources at walls, raising its density. In both cases, dissociation fraction is large.



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• Without wall passivation, sources Cl<sub>2</sub> from the walls are larger, resulting in more dissociative attachment and lower [e].



## **EXAMPLES OF NON-EQUILIBRIUM**

- Electromagnetic non-equilibrium: Anomalous skin depth
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#### MICRODISCHARGE PLASMA SOURCES

- Microdischarges are plasma devices which leverage pd scaling to operate dc atmospheric glows 10s  $-100s \ \mu m$  in size.
- MEMS fabrication techniques enable innovative structures for displays and detectors.
- Although similar to PDP cells, MDs are dc devices which largely rely on nonequilibrium beam components of the EED.
- Electrostatic nonequilibrium results from their small size. Debye lengths and cathode falls are commensurate with size of devices.

$$L_{cathode Fall} = \left(\frac{2V_c \varepsilon_0}{(qn_I)}\right)^{1/2} \approx 10 - 20 \,\mu m$$
$$\lambda_D \approx 750 \left(\frac{T_{eV}}{n_e (cm^{-3})}\right)^{1/2} cm \approx 10 \,\mu m,$$

## **PYRAMIDAL MICRODISCHARGE DEVICES**

- Si MDs with 10s  $\mu$ m pyramidal cavities display nonequilibrium behavior: Townsend to negative glow transitions.
- Small size also implies electrostatic nonequilibrium.





 S.-J. Park, et al., J. Sel. Topics Quant. Electron 8, 387 (2002); Appl. Phys. Lett. 78, 419 (2001).

#### **2-D MODELING OF MICRODISCHARGE SOURCES**

• Charged particle continuity (fluxes by Sharfetter-Gummel form)

$$\frac{\partial N_i}{\partial t} = -\vec{\nabla} \cdot \left( qN_i \mu_i \left( -\vec{\nabla} \Phi \right) - D_i \nabla N_i \right) + S_i$$

• Poisson's Equation for Electric Potential

$$-\nabla \cdot \varepsilon \nabla \Phi = \rho_V + \rho_S$$

• Bulk continuum electron energy transport and MCS beam.

$$\frac{\partial(n_e\varepsilon)}{\partial t} = \vec{j} \cdot \vec{E} - n_e \sum_i N_i \kappa_i - \nabla \cdot \left(\frac{5}{2}\varepsilon\varphi - \lambda\nabla T_e\right), \quad \vec{j} = q\vec{\phi}_e$$

• Neutral continuity and energy transport.

$$\frac{\partial N_i}{\partial t} = -\nabla \cdot \left( \vec{v} - DN_o \nabla \left( \frac{N_i}{N_o} \right) \right) + S_i, \quad \frac{\partial (\rho cT)}{\partial t} = -\nabla \cdot \kappa \nabla T + P_g$$

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• Transport of energetic secondary electrons is addressed with a Monte Carlo Simulation.



- Superimpose Cartesian MCS mesh on unstructured fluid mesh. Construct Greens functions for interpolation between meshes.
- Electrons and their progeny are followed until slowing into bulk plasma or leaving MCS volume.
- Electron energy distribution is computed on MCS mesh.
- EED produces source functions for electron impact processes which are interpolated to fluid mesh.

#### **MODEL GEOMETRY: SI PYRAMID MICRODISCHARGE**

Investigations of a cylindrically symmetric Si pyramid MD.
 Typical meshes have 5,000-10<sup>4</sup> nodes, dynamic range of 50-100.



#### BASE CASE: Ne, 600 Torr, 50 $\mu$ m DIAMETER



- Optimum conditions produces large enough charge density to warp electric potential into cathode well.
- In spite of large Te, ionization is dominated by beam electrons.

• Ne, 600 Torr, 50  $\mu m$  diameter, 200 V, 1 M $\Omega$ 

### **BASE CASE: CHARGED PARTICLE DENSITIES**



- There are few regions of quasi-neutrality or which are positive column-like.
- [e] >  $10^{13}$  cm<sup>-3</sup> for 10s  $\mu$ A.
- Excited state densities >10<sup>15</sup> cm<sup>-3</sup> are commensurate with macroscopic pulsed discharge devices.

#### **ELECTRON DENSITY vs PRESSURE**



• The discharge becomes more confined at higher pressures due to shorter stopping length of beam electrons.

#### **BEAM vs BULK: NONEQUILIBRIUM IONIZATION SOURCES**

- The threshold for Ne  $\rightarrow$  Ne<sup>++</sup> is 41 eV. Monitoring S[Ne<sup>++</sup>]/S[Ne<sup>+</sup>] signals MD transitions from Townsend-like to negative glow-like.
- Negative glow-like excitation occurs with P < 550 Torr.



- Pd scaling should not be a steadfast expectation.
- Sheath properties scale with absolute plasma density and not pd.
- Scaling requires careful ballasting to keep [e] and sheath



• When keeping ballast constant, j decreases in larger devices, resulting in lower electron density, less shielding, more "electrostatic" equilibrium. Electron cloud "pops" out of cavity.



• Ne, 200 V, 1 MΩ

#### **CONCLUDING REMARKS and ACKNOWLEDGEMENTS**

- Nonequilibrium in plasma processing is everywhere you look...
  - Electromagnetics
  - Plasma dynamics
  - Surface chemistry
  - Electrostatics
- The development of computational and experimental techniques to resolve non-equilibrium will continue to be important in improving our fundamental understanding of these processes.
- Collaborators
  - Dr. Alex Vasenkov
  - Mr. Arvind Sankaran

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